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## A procedure for estimating a few demographic indicators of Assam state and its districts

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### Abstract

In India, as vital statistics reports bear flaws due to incomplete and irregular birth and death registration, researchers resort to the use of various indirect techniques of demographic estimation. In this regard, challenges faced by researchers in the area lie in the development effective indirect techniques of estimation. This paper has proposed a five parameters polynomial regression model for estimating the life expectancy at birth using child survivorship probabilities obtained from indirect techniques of estimation of infant and child mortality rates. Estimates of life expectancies at birth, infant mortality rates, under age five mortality rates and life expectancies at birth at sub-state level, i.e., district level of Assam, obtained in this paper, may provide a set of demographic indicators enormously useful to health and socio-economic planners of the state. Logit smoothing is done to child mortality estimates given by Trussell's variant of Brass methods on children ever born (CEB) and children surviving (CS) of 2001 and 2011 census of India, and then Weibull survival function is fitted to the smoothed estimates so as to finally obtain infant and child mortality estimates with enhanced precision. A procedure is adopted here in selecting a suitable model life table family in which two established techniques are simultaneously used. MORTPAK for Windows, the UN software package for demographic measurement in developing countries, is used in abridged life tables of Assam - 23 each for male, female and the combined, from 1970 to 2016, to get unabridged life tables from the abridged wherever required.

**Keywords:** Infant mortality rates (IMR), under five mortality rates (U5MR), life expectancy at birth

### 1. Introduction

Life expectancy at birth ( ${}^e_0$ ), i.e., the longevity of a new born based on age-specific death rates, is an important indicator to determine the mortality level of a population from which demographers can draw an idea about the socio-economic condition and health status of that particular population (Najafi, *et al.*, 2018, Motlagh, *et al.*, 2012) <sup>[7, 6]</sup>. However, life expectancies at ages other than zero are also used for studying mortality pattern of cohort population. In the case of most developing countries and historical populations, high incidence of infant and child mortality results in lower values of  ${}^e_0$  than at other childhood ages, and in such populations, those surviving the hazards of early childhood have a higher life expectancy than new born and the highest life expectancy does not occurs at birth but at later age (Romo and Becker, 2011) <sup>[9]</sup>.

Phukon and Ahamed (2019) <sup>[8]</sup> estimated life expectancy at birth by developing two polynomial regression models comprising child survivorship probabilities at ages one, two, three and four, i.e.,  $l_1$ ,  $l_2$ ,  $l_3$  and  $l_4$  using 54 set of SRS based abridged life tables of Assam. Prior to this, Romo and Becker (2011) <sup>[9]</sup> and Sarma and Choudhury (2012) <sup>[11]</sup> had estimated the life expectancy at birth by developing the linear and quadratic regression models between  ${}^e_0$  and survivorship function at age one respectively. In some of the earlier literatures, it can always be found that  ${}^e_0$  is somehow inextricably related to life expectancies at childhood ages. In retrospect, Lederman (1969) <sup>[5]</sup> developed a series of one parameter and two parameters regression models, and thus a number of life tables were constructed based on such models; the author proposed model life tables by generating the logarithmic regression equation between probability of dying at ages  $x$  and  $(x+5)$ .

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A number of sets of regression coefficients for each equation based on different independent variables (e.g.,  ${}^e_0$ ,  $1q_0$ ,  $5q_0$ ,  $15q_0$ ,  $20q_{30}$ ,  $20q_{45}$  and  $m50+$ ) or a pair of variables were obtained.

Hence, it can be observed that  ${}^e_0$  is also indispensably influenced by mortality conditions in childhood ages. Roy (1989) [10] obtained reliable estimates of child survivorship functions,  $l_x = 1 - q_x$ , for India using logit smoothing.

In this paper, a five parameters polynomial regression model  $e_0(t) = \lambda + \gamma l_1 + \delta l_2 + \phi l_3 + \psi l_3^2$ , where  $l_1$ ,  $l_2$  and  $l_3$  are the survival probabilities at childhood ages one, two and three, have been derived. The model gives relationship, in the particular case of Assam, between  ${}^e_0$  and the survival probabilities  $l_1$ ,  $l_2$  and  $l_3$  by fitting polynomial regression on aforesaid SRS data of Assam. Life expectancy at birth is estimated by using the fitted model as the estimating equation Assam. With the sequential application of Trussell's variant of Brass method, logit smoothing and fitting of Weibull survival function (Sarma and Choudhury, 2012, 2014) [11, 12] at district level of Assam, estimates of  $l_1$ ,  $l_2$  and  $l_3$  from CEB and CS census data of 2001 and 2011 are obtained and these estimates are substituted in the estimating equations for estimating  ${}^e_0$ . The estimated values of  ${}^e_0$ , infant mortality rate (IMR), and under five mortality rate (U5MR) are presented in Table 2-4.

**2. Materials and Methods**

In this paper, 69 sets of SRS-based abridged life tables of Assam, which was published by office of the Registrar General of India, from 1970-75 to 2012-16, 23 each for male,

female, and male and female combined are used. The polynomial regression model proposed in this paper is fitted to this SRS data of Assam. For estimating the demographic parameters such as,  ${}^e_0$ , IMR and U5MR for sub-state level of Assam, CEB, CS and total numbers of women in child bearing ages are taken from Indian Census data of 2001 and 2011 of Assam. Moreover, in selecting suitable standard model life table for Assam, each of five United Nations model life tables for developing countries (1983) [13] and four Princeton models-Coale & Demeny model life tables (1966) [3] is examined to find out which standard model is most appropriate for Assam.

**2.1 Selection of a Model Life Table Family for Multipliers**

The appropriate model life table family has been selected by using the following procedure.

At first, in graphical method, the estimates of  ${}_4q_1$  are plotted against those of  $1q_0$  (Kenneth, 2013) [4] on a graph showing the corresponding relationships in model life tables, shown in Figure 1. Although observed data of Assam reflects trivial nature in this graphical representation, somehow the graph of model life table which is closely fitted to that of observed data

is selected. Secondly, we calculate  $\sum_{L=1}^n \left(1 - \frac{m_x}{M_x}\right)^2$ , where

$m_x$  is the Age Specific Mortality Rate (ASMR) of observed data,  $M_x$  is the ASMR of standard life table, L is the level that corresponds to that of observed data. The model set that minimizes the sum is taken as appropriate model life. In both methods, Assam's SRS data is found to be most compatible with United Nations South Asian model life tables.

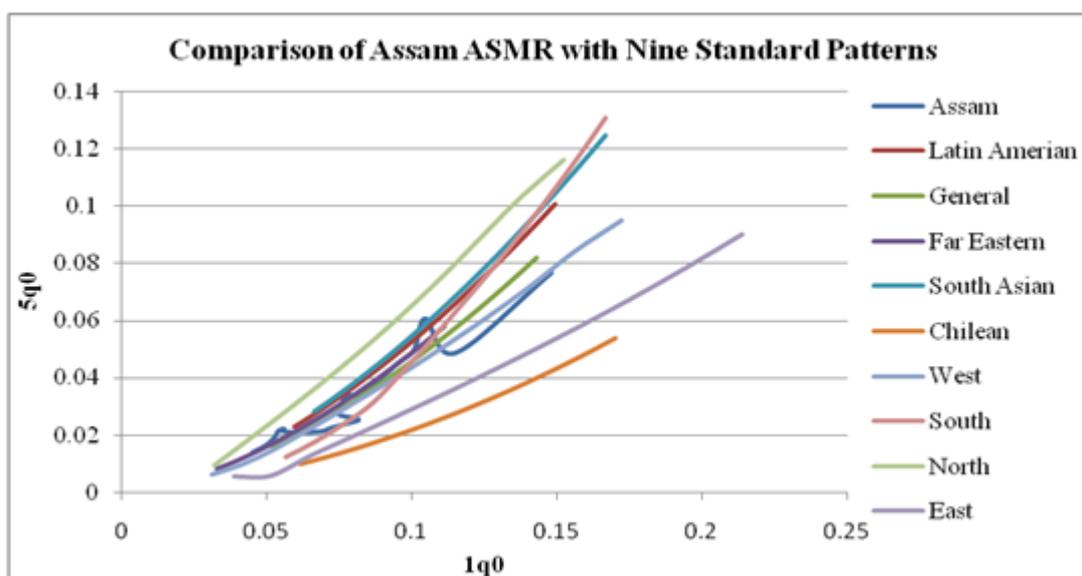


Fig 1: Child mortality patterns of Assam with those of nine standard model life tables

**2.2 Trussell's Variant of Brass Method**

Brass developed a method for converting the proportions dead of children ever born reported by women in childbearing ages into estimates of the probability of dying whereas translating proportions of children dead among children ever born into standard life table indicators was first pioneered by Brass and Coale (1968) [1]. If mortality has changed over time, the estimated probabilities of dying reflect the mortality rates that

have prevailed at a range of ages and dates. The following steps are followed in estimating probability of dying.

The average parity per woman is computed by using  $P(i) = CEB(i)/N(i)$ , where CEB is the children ever born for age group  $i$ ,  $i = 1, 2, \dots, 7$  for age-groups called child bearing age groups, i.e., 15-19, 20-24, ... 45-49 respectively and  $N(i)$  is the total number of women of the age-groups. The proportion of children dead for each age-group  $i$  is estimated

as  $D(i) = (CEB(i) - CS(i)) / CEB(i)$  and  $CD(i) / CEB(i)$ , where  $CS(i)$  is the number of children surviving for the age-group  $i$  and  $CD(i)$  is the children dead reported by the mothers belonging to the age-group  $i$ . The multipliers  $K(i)$  are computed according to the Trussell's variant of original Brass method. Equations are obtained as  $K(i) = a(i) + b(i) * P_1 / P_2 + c(i) * P_2 / P_3$ , where  $a(i)$ ,  $b(i)$  and  $c(i)$  are coefficients for estimation of child mortality multipliers, which is taken from United Nations (1983)<sup>[13]</sup> South Asian model in this context. Multiplier is the factor to convert the proportion of children dead into a probability of dying which will be estimated by using,  $q_x = K(i) * D(i)$ .

**2.3 Weibull Survival Function**

The survival probability function for age  $x$  of Weibull distribution is  $l_x = e^{-\alpha x^\beta}$ ;  $\alpha > 0, \beta > 0$ , and  $x \geq 0$  (Choe, 1981)<sup>[2]</sup>; it can be written as  $\ln(\ln(1/l(x))) = \ln \alpha + \beta * \ln(x)$ . We can also obtain  $q_x = 1 - l_x = 1 - e^{-\alpha x^\beta}$ . Initially  $l_x$  values for  $x = 1, 2, 3, 5$  are estimated by using Trussell's variant of Brass method on CEB and CS data of Assam for census 2001 and 2011. Then, the estimated values of  $l_x$  are made monotonically decreasing through logit smoothing in which we suppose  $P_x = \log it(l_x)$ , where  $\log it(l_x) = 0.5 * \ln(1 - l_x / l_x)$ .

The smoothed values of  $P_x$  are obtained from  $\hat{P}_x = P_x^s + (1/3) \sum_{x=2,3,5} \{P_x - P_x^s\}$ .  $P_x^s$  is the Brass logit standard values taken from Brass logit tables for  $x=2,3, 5$  (Roy, 1989)<sup>[10]</sup>. Using the smoothed values of  $\hat{P}_x$ ,  $l_x$  can be finally estimated by using the relation  $\hat{l}_x = 1 / (1 + e^{2\hat{P}_x})$ .

These  $\hat{l}_x$  values are used in the polynomial regression model fitted to SRS data of Assam to estimate life expectancies at birth for the state of Assam and her all districts.

**2.4 Polynomial Regression Model**

A second degree polynomial regression model has been derived by establishing the relationship between the life expectancy at birth,  $e_0$  and the survivorship probabilities  $l_1, l_2$  and  $l_3$ . Considering the equations used by Romo and Becker (2011)<sup>[9]</sup> and Sarma and Choudhury (2012)<sup>[11]</sup> respectively as follows:

$$e_0(t) = {}_1L_0(t) + e_1(t)l_1(t) \tag{1}$$

$$e_0 = a + (b + c)l_1 + dl_1^2 \tag{2}$$

where  ${}_1L_0(t)$  is the person-years lived between birth and age

one,  $e_1(t)$  is the life expectancy at age one and  $l_1(t)$  is the probability of survivorship function at age one.

The equation (1) can be extended as

$$e_0(t) = \int_0^1 l(\alpha, t) d\alpha + \int_1^2 l(\alpha, t) d\alpha + \int_2^3 l(\alpha, t) d\alpha + \int_3^\eta l(\alpha, t) d\alpha$$

where  $\eta$  is the highest age attained by a member of population.

Considering the effect of childhood mortality changes in age interval (0-3) on  $e_0$ , the following equation can be obtained:

$$e_0(t) = {}_1L_0(t) + {}_1L_1(t) + {}_1L_2(t) + e_3 * l_3(t)$$

${}_1L_0(t)$  is a weighted linear function of  $l_1(t)$  and so also  ${}_1L_1(t)$  and  ${}_1L_2$  are a weighted linear function of  $l_1(t), l_2(t)$  and  $l_2(t), l_3(t)$  respectively. Moreover By assuming  $e_3(t)$  as a linear function of  $l_3(t)$ , the above equation may be expressed as:

$$e_0 = f + g * l_1 + h * l_1 + i * l_2 + j * l_2 + (m + n l_3) * l_3$$

$$e_0(t) = \lambda + \gamma * l_1 + \delta * l_2 + \phi * l_3 + \psi * l_3^2 \tag{3}$$

where,  $\lambda, \gamma, \delta, \phi$ , and  $\psi$  are the five parameters (regression coefficients) of the second degree polynomial equation. The assumption that  $e_3(t)$  is linear function of  $l_3(t)$  has got its perspective from the empirical examination results shown in Table 5. It is seen from this table that Pearson correlation co-efficient between  $e_3(t)$  and  $l_3(t)$  in all model life table families are exceptionally high. It is also known that Pearson correlation coefficients are often used as an indicator of strength of linearity between two variables. Moreover, the consistency of this assumption is reflected in the final results given by the model constructed based on the assumptions.

**3. Results**

Table 1 is presents fitted polynomial regression models along with coefficients of determination ( $R^2$ ) and standard errors (SE), in each case, in all five United Nations model life tables and four Princeton-Coale & Demeny's model life tables sex-wise, and also for Assam sex-wise as well as total of male and female. The goodness of fit has been seen from the high coefficients of determination and low standard errors of fitting in all model life table families and SRS life tables of Assam. It is analytically justifiable that the polynomial regression model constructed based on certain assumptions and mathematical formulation of vital statistics works realistically in estimating life expectancy at birth. Tables 2 to 4 present the estimated life expectancies at birth, IMRs and U5MRs of Assam and its districts in 2001 and 2011 along with their percentage increase/decrease respectively.

**Table 1:** Polynomial Regression Models fitted to SRS data of Assam and model life table families

| Life Tables     |        | Polynomial Regression Model                              |  |  | R <sup>2</sup> | SE     |
|-----------------|--------|--|--|--|----------------|--------|
| Chilean Pattern | Male   | $49.41+614.42l_1-1428.72l_2+634.28l_3+210.28l_3^2$       |  |  | 0.9993         | 0.3423 |
|                 | Female | $-254.10+2061.84l_1-4238.11l_2+2513.2l_3+3.76l_3^2$      |  |  | 0.9999         | 0.0447 |
| Far Eastern     | Male   | $-790.47+1512.22l_1+256.62l_2-621.84l_3-277.1l_3^2$      |  |  | 0.9998         | 0.1640 |
|                 | Female | $-427.49+6014.31l_1-13713.64l_2+8013.07l_3+201.02l_3^2$  |  |  | 0.9995         | 0.2962 |
| General Pattern | Male   | $-290.60+3580.38l_1-8229.1l_2+4980.08l_3+41.12l_3^2$     |  |  | 0.9999         | 0.0661 |
|                 | Female | $5.33+5656.13l_1-14366.41l_2+8350.93l_3+440.56l_3^2$     |  |  | 0.9998         | 0.1770 |
| Latin American  | Male   | $-283.11+266.65l_1+1155.45l_2-1064.76l_3+10.88l_3^2$     |  |  | 0.9999         | 0.0675 |
|                 | Female | $-195.50+2337.21l_1-4895.44l_2+2644.84l_3+196.73l_3^2$   |  |  | 0.9999         | 0.0213 |
| South Asian     | Male   | $-233.03+2066.37l_1-4402.85l_2+2603l_3+49.4l_3^2$        |  |  | 0.9999         | 0.0442 |
|                 | Female | $-135.92-128.11l_1+1045.95l_2-727.42l_3+29.59l_3^2$      |  |  | 0.9999         | 0.0767 |
| East Model      | Male   | $-65.04+3665.74l_1-10700.73l_2+7147.2l_3+29.489l_3^2$    |  |  | 0.9998         | 0.3235 |
|                 | Female | $-1.69.23+6216.15l_1-16475.51l_2+10438.67l_3+72.14l_3^2$ |  |  | 0.999          | 0.2354 |
| North Model     | Male   | $-117.89+1183.88l_1-1534.84l_2+318.97l_3+231.48l_3^2$    |  |  | 0.9999         | 0.2235 |
|                 | Female | $-72.94+189.8l_1+1107.67l_2-1434.27l_3+299.12l_3^2$      |  |  | 0.9998         | 0.2683 |
| South Model     | Male   | $-35.43+216.55l_1-138.05l_2-92.47l_3+132.44l_3^2$        |  |  | 0.9999         | 0.1087 |
|                 | Female | $9.03-112.76l_1+504.56l_2-468.1l_3+152.78l_3^2$          |  |  | 0.9999         | 0.1561 |
| West Model      | Male   | $-119.96+3487.3l_1-9605.35l_2+6265.76l_3+40.47l_3^2$     |  |  | 0.9999         | 0.1884 |
|                 | Female | $-65.12+537.03l_1+39.77l_2-666.18l_3+235.54l_3^2$        |  |  | 0.9998         | 0.2593 |
| Assam           | Male   | $77.22+113l_1-614.04l_2+356.7l_3+139.02l_3^2$            |  |  | 0.9880         | 0.5343 |
|                 | Female | $-61.06+527.79l_1-1396.04l_2+940.79l_3+67.03l_3^2$       |  |  | 0.9969         | 0.3384 |
|                 | Total  | $56.51+236.56l_1-739.26l_2+357.98l_3+163.69l_3^2$        |  |  | 0.9937         | 0.4354 |

**Table 2:** Percentages of increase/decrease in Life Expectancy at Birth ( $e_0$ ), Assam and its Districts

| Districts     | Male           |                |                       | Female         |                |                       | Total          |                |                       |
|---------------|----------------|----------------|-----------------------|----------------|----------------|-----------------------|----------------|----------------|-----------------------|
|               | $e_0$ for 2001 | $e_0$ for 2011 | Increase/Decrease (%) | $e_0$ for 2001 | $e_0$ for 2011 | Increase/Decrease (%) | $e_0$ for 2001 | $e_0$ for 2011 | Increase/Decrease (%) |
| Kokrajhar     | 57.14          | 60.12          | 5.21                  | 58.61          | 55.48          | -5.34                 | 58.07          | 60.29          | 3.82                  |
| Dhubri        | 53.12          | 56.53          | 6.43                  | 54.21          | 58.25          | 7.45                  | 53.86          | 57.56          | 6.87                  |
| Goalpara      | 54.94          | 59.02          | 7.42                  | 57.27          | 60.12          | 4.98                  | 56.19          | 59.81          | 6.45                  |
| Bongaigaon    | 55.64          | 59.16          | 6.34                  | 57.43          | 63.72          | 10.95                 | 56.67          | 61.41          | 8.35                  |
| Barpeta       | 56.12          | 60.01          | 6.93                  | 58.26          | 59.50          | 2.14                  | 57.31          | 60.13          | 4.93                  |
| Kamrup        | 59.15          | 59.90          | 1.27                  | 61.88          | 63.96          | 3.36                  | 60.63          | 61.94          | 2.17                  |
| Darrang       | 54.01          | 56.82          | 5.20                  | 54.93          | 60.85          | 10.76                 | 54.69          | 58.79          | 7.48                  |
| Marigaon      | 55.80          | 57.40          | 2.86                  | 58.69          | 59.67          | 1.67                  | 57.28          | 58.66          | 2.41                  |
| Nagaon        | 56.38          | 58.61          | 3.95                  | 58.58          | 61.88          | 5.64                  | 57.59          | 60.30          | 4.69                  |
| Sonitpur      | 57.18          | 59.40          | 3.88                  | 59.77          | 59.07          | -1.17                 | 58.56          | 59.60          | 1.76                  |
| Lakhimpur     | 58.50          | 60.87          | 4.06                  | 61.83          | 62.74          | 1.48                  | 60.21          | 62.02          | 3.00                  |
| Dhemaji       | 59.02          | 53.81          | -8.82                 | 62.20          | 53.13          | -14.57                | 60.67          | 52.39          | -16.2                 |
| Tinsukia      | 61.26          | 62.06          | 1.31                  | 65.04          | 64.70          | -0.53                 | 63.22          | 63.56          | 0.53                  |
| Dibrugarh     | 62.94          | 60.62          | -3.70                 | 66.30          | 65.56          | -1.11                 | 64.76          | 63.49          | -1.97                 |
| Sivasagar     | 58.39          | 59.90          | 2.58                  | 61.51          | 65.32          | 6.20                  | 60.01          | 62.50          | 4.15                  |
| Jorhat        | 60.22          | 61.23          | 1.68                  | 63.38          | 66.23          | 4.49                  | 61.89          | 63.69          | 2.90                  |
| Golaghat      | 60.15          | 59.93          | -0.35                 | 63.30          | 64.65          | 2.12                  | 61.82          | 62.25          | 0.69                  |
| Karbi Anglong | 56.49          | 57.84          | 2.38                  | 57.55          | 59.62          | 3.61                  | 57.25          | 58.91          | 2.90                  |

|                               |       |       |       |       |       |      |       |       |      |
|-------------------------------|-------|-------|-------|-------|-------|------|-------|-------|------|
| North Cachar Hills/Dima Hasao | 58.55 | 60.83 | 3.88  | 60.11 | 64.06 | 6.56 | 59.53 | 62.45 | 4.91 |
| Cachar                        | 54.81 | 59.93 | 9.35  | 58.41 | 63.90 | 9.40 | 57.34 | 61.93 | 8.00 |
| Karimganj                     | 56.07 | 57.38 | 2.33  | 55.59 | 60.77 | 9.32 | 55.42 | 59.09 | 6.63 |
| Hailakandi                    | 56.35 | 55.78 | -1.01 | 57.47 | 60.23 | 4.81 | 57.13 | 57.87 | 1.30 |
| Chirang                       | -     | 59.54 | -     | -     | 62.42 | -    | -     | 61.08 | -    |
| Kamrup Metro                  | -     | 61.57 | -     | -     | 64.67 | -    | -     | 63.99 | -    |
| Baksa                         | -     | 60.12 | -     | -     | 62.99 | -    | -     | 61.68 | -    |
| Udalguri                      | -     | 58.16 | -     | -     | 62.70 | -    | -     | 60.36 | -    |
| Nalbari                       | 58.36 | 61.73 | 5.77  | 61.06 | 65.87 | 7.87 | 59.81 | 63.85 | 6.76 |
| Assam                         | 56.66 | 59.16 | 4.41  | 58.50 | 61.87 | 5.76 | 58.34 | 60.63 | 3.93 |

**Table 3:** Percentages of increase/decrease in Infant Mortality Rate (IMR), Assam and its Districts

| Districts                     | Male         |              |                       | Female       |              |                       | Total        |              |                       |
|-------------------------------|--------------|--------------|-----------------------|--------------|--------------|-----------------------|--------------|--------------|-----------------------|
|                               | IMR for 2001 | IMR for 2011 | Increase/Decrease (%) | IMR for 2001 | IMR for 2011 | Increase/Decrease (%) | IMR for 2001 | IMR for 2011 | Increase/Decrease (%) |
| Kokrajhar                     | 71           | 73           | 3.12                  | 70           | 82           | 17.14                 | 71           | 78           | 10.18                 |
| Dhubri                        | 94           | 74           | -21.22                | 88           | 72           | -17.89                | 91           | 73           | -19.65                |
| Goalpara                      | 83           | 61           | -27.23                | 76           | 65           | -14.33                | 80           | 63           | -21.11                |
| Bongaigaon                    | 79           | 60           | -24.48                | 75           | 52           | -31.44                | 77           | 56           | -27.92                |
| Barpeta                       | 77           | 55           | -27.58                | 72           | 67           | -6.57                 | 74           | 61           | -17.40                |
| Kamrup                        | 60           | 56           | -6.56                 | 58           | 51           | -13.14                | 59           | 53           | -9.76                 |
| Darrang                       | 89           | 73           | -18.24                | 85           | 62           | -26.71                | 87           | 68           | -22.35                |
| Marigaon                      | 78           | 69           | -11.42                | 70           | 67           | -5.30                 | 74           | 68           | -8.60                 |
| Nagaon                        | 75           | 63           | -16.30                | 71           | 58           | -17.58                | 73           | 61           | -16.90                |
| Sonitpur                      | 71           | 59           | -16.95                | 66           | 69           | 4.01                  | 69           | 64           | -6.86                 |
| Lakhimpur                     | 63           | 51           | -19.63                | 59           | 55           | -5.79                 | 61           | 53           | -13.05                |
| Dhemaji                       | 61           | 90           | 48.37                 | 57           | 92           | 60.93                 | 59           | 89           | 49.15                 |
| Tinsukia                      | 49           | 45           | -8.23                 | 47           | 48           | 2.68                  | 48           | 46           | -2.96                 |
| Dibrugarh                     | 41           | 52           | 28.74                 | 42           | 45           | 6.30                  | 41           | 47           | 12.93                 |
| Sivasagar                     | 64           | 56           | -12.49                | 60           | 46           | -23.50                | 62           | 51           | -17.65                |
| Jorhat                        | 54           | 49           | -9.52                 | 53           | 42           | -19.65                | 54           | 46           | -14.37                |
| Golaghat                      | 55           | 56           | 2.02                  | 53           | 48           | -9.28                 | 54           | 52           | -3.45                 |
| Karbi Anglong                 | 74           | 67           | -10.01                | 75           | 67           | -10.59                | 75           | 67           | -10.29                |
| North Cachar Hills/Dima Hasao | 63           | 51           | -18.86                | 65           | 50           | -22.55                | 64           | 51           | -20.11                |
| Cachar                        | 84           | 56           | -33.61                | 72           | 51           | -28.75                | 74           | 53           | -27.92                |
| Karimganj                     | 77           | 69           | -9.52                 | 82           | 63           | -24.08                | 83           | 66           | -20.72                |
| Hailakandi                    | 75           | 78           | 4.31                  | 75           | 65           | -14.01                | 75           | 72           | -4.61                 |
| Chirang                       | -            | 58           | -                     | -            | 56           | -                     | -            | 57           | -                     |
| Kamrup Metro                  | -            | 47           | -                     | -            | 48           | -                     | -            | 45           | -                     |
| Baksa                         | -            | 55           | -                     | -            | 54           | -                     | -            | 55           | -                     |
| Udalguri                      | -            | 65           | -                     | -            | 55           | -                     | -            | 60           | -                     |
| Nalbari                       | 64           | 47           | -27.28                | 62           | 44           | -28.80                | 63           | 45           | -28.01                |
| Assam                         | 71           | 60           | -15.89                | 71           | 58           | -17.85                | 70           | 59           | -14.90                |

**Table 4:** Percentages of increase/decrease in Under Five Mortality Rate (U5MR), Assam and its Districts

| Districts  | Male          |               |                       | Female        |               |                       | Total         |               |                       |
|------------|---------------|---------------|-----------------------|---------------|---------------|-----------------------|---------------|---------------|-----------------------|
|            | U5MR for 2001 | U5MR for 2011 | Increase/Decrease (%) | U5MR for 2001 | U5MR for 2011 | Increase/Decrease (%) | U5MR for 2001 | U5MR for 2011 | Increase/Decrease (%) |
| Kokrajhar  | 109           | 113           | 3.46                  | 109           | 127           | 16.26                 | 109           | 120           | 9.86                  |
| Dhubri     | 143           | 114           | -20.30                | 134           | 111           | -17.13                | 139           | 113           | -18.80                |
| Goalpara   | 128           | 94            | -26.25                | 117           | 101           | -13.78                | 122           | 97            | -20.33                |
| Bongaigaon | 122           | 93            | -23.61                | 116           | 81            | -30.47                | 119           | 87            | -26.99                |
| Barpeta    | 118           | 86            | -26.68                | 111           | 104           | -6.31                 | 114           | 95            | -16.77                |
| Kamrup     | 93            | 87            | -6.34                 | 91            | 79            | -12.75                | 92            | 83            | -9.45                 |
| Darrang    | 136           | 112           | -17.46                | 130           | 97            | -25.72                | 133           | 104           | -21.46                |
| Marigaon   | 120           | 107           | -10.96                | 109           | 103           | -5.09                 | 115           | 105           | -8.26                 |
| Nagaon     | 115           | 97            | -15.70                | 109           | 91            | -16.97                | 113           | 94            | -16.29                |
| Sonitpur   | 109           | 91            | -16.36                | 103           | 107           | 3.85                  | 106           | 99            | -6.60                 |
| Lakhimpur  | 98            | 80            | -19.04                | 91            | 86            | -5.60                 | 95            | 83            | -12.63                |
| Dhemaji    | 94            | 137           | 45.83                 | 89            | 140           | 57.66                 | 92            | 139           | 51.08                 |
| Tinsukia   | 77            | 70            | -8.01                 | 73            | 75            | 2.61                  | 75            | 73            | -2.88                 |
| Dibrugarh  | 64            | 82            | 27.84                 | 66            | 70            | 6.13                  | 65            | 73            | 12.57                 |
| Sivasagar  | 99            | 87            | -12.07                | 93            | 72            | -22.86                | 96            | 80            | -17.12                |
| Jorhat     | 85            | 77            | -9.24                 | 82            | 67            | -19.15                | 84            | 72            | -13.97                |

|                               |     |     |        |     |     |        |     |     |        |
|-------------------------------|-----|-----|--------|-----|-----|--------|-----|-----|--------|
| Golaghat                      | 85  | 87  | 1.95   | 83  | 75  | -9.01  | 84  | 81  | -3.34  |
| Karbi Anglong                 | 115 | 104 | -9.61  | 115 | 103 | -10.17 | 115 | 104 | -9.89  |
| North Cachar Hills/Dima Hasao | 98  | 80  | -18.29 | 101 | 79  | -21.87 | 99  | 80  | -19.50 |
| Cachar                        | 129 | 87  | -16.67 | 110 | 80  | -12.06 | 114 | 83  | -10.48 |
| Karimganj                     | 118 | 107 | 2.06   | 126 | 97  | -20.78 | 128 | 102 | -13.41 |
| Hailakandi                    | 116 | 120 | -30.92 | 116 | 100 | -31.94 | 116 | 111 | -30.91 |
| Chirang                       | -   | 90  | -      | -   | 88  | -      | -   | 89  | -      |
| Kamrup Metro                  | -   | 74  | -      | -   | 75  | -      | -   | 70  | -      |
| Baksa                         | -   | 85  | -      | -   | 85  | -      | -   | 85  | -      |
| Udalguri                      | -   | 101 | -      | -   | 86  | -      | -   | 94  | -      |
| Nalbari                       | 99  | 73  | -26.52 | 95  | 69  | -28.04 | 97  | 71  | -27.25 |
| Assam                         | 110 | 93  | -15.33 | 110 | 91  | -17.23 | 107 | 92  | -14.37 |

**Table 5:** Pearson’s Correlation coefficients between  $e_3$  and  $l_3$  for model life tables and SRS life tables of Assam

| Model  | United Nations Model Life Tables |             |         |                |             | Princeton-Coale & Demeny Model Life Table |        |        |        | Assam: SRS-based Abridged Life Table |
|--------|----------------------------------|-------------|---------|----------------|-------------|---|--------|--------|--------|--------------------------------------|
|        | Chilean                          | Far Eastern | General | Latin American | South Asian | East                                      | North  | South  | West   |                                      |
| Male   | 0.9690                           | 0.9822      | 0.9917  | 0.9945         | 0.9956      | 0.9885                                    | 0.9851 | 0.9927 | 0.9855 | 0.9755                               |
| Female | 0.9981                           | 0.9740      | 0.9971  | 0.9980         | 0.9987      | 0.9868                                    | 0.9861 | 0.9940 | 0.9848 | 0.9730                               |
| Total  | -                                | -           | -       | -              | -           | -   | -      | -      | -      | 0.9898                               |
| Levels | 41                               | 41          | 41      | 41             | 41          | 25  | 25     | 25     | 25     | 23                                   |

**4. Discussion and Conclusion**

It is worth-noting that the estimation of life expectancy at birth ( $e_0$ ), IMR and U5MR are the key demographic measures of health status and socio-economic conditions of a country. Tables 2 to 4 present life expectancy at birth, IMR and U5MR, which are defined in terms of probability of dying before reaching of one’s first and fifth birthday anniversary respectively, calculated per 1000 live births, for Assam and its districts as per Censuses 2001 and 2011.

When we look into the estimated gain or loss of life expectancy district-wise and sex-wise in Assam, Table 2 shows, in most cases, female life expectancies are a matter of serious concern. Dhemaji is predominantly tribal populated area in which a sheer decrease of life expectancies of females (14.57%) is seen. Moreover, Barpeta, Sonitpur and Dibrugarh have shown decrease in female life expectancies, whereas Golaghat, Hailakandi, Kamrup have shown drop in life expectancies of males. If we look at Assam as a whole, there is increase of life expectancy by 3.93% for persons, 4.41% for males and 5.76% for females.

Regarding the increase and decrease of IMR, for Assam state as a whole, IMR decreases: 15.89% for males, 17.85% for females and 14.90% for persons. However, when we look into the state of affairs district-wise, Kokrajhar, Dibrugarh, Dhemaji and Tinsukia (for females) have shown increasing IMR among which Dibrugarh and Dhemaji districts have shown exceptional increase.

Under-five mortality rate is also another good indicator of vital statistics. In the regions where socio-economic condition is relatively backward and adequate child care incentives are not available, usually children under age five are prone to sickness and death. When we look at the scenario of Assam and its districts from this aspect of demographic determinant, the state as a whole has shown decrease in U5MR by 15.33% for male, 17.23% for female, and 14.37% for person. But in the districts Kokrajhar, Dhemaji, Dibrugarh, Karimganj, Sonitpur and Tinsukia, we have seen increase in U5MR. Most of these districts are tribal majority populated areas. It calls for proper investigation that whether child health care facilities, immunization and adequate nutrition are available without discrimination in these areas.

The state development planners have to initiate inward-looking substantial measures. The existing disparities must be fairly addressed. The results provided in this paper in the form of research findings may provide insight comprehensively into a few components of human development index in Assam. Tribal inhabited areas and flood prone districts have shown serious problems. High disparity shown in terms of human development factors is a matter of serious concern.

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