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Performance criteria of modified multihalver technique for detecting outlying values of body mass index (BMI): A higher risk factor and prognosis of COVID-19 infections

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Abstract

The detection of outlier (s) is often thought of as a means to eliminate such aberrant observation(s) from a set of data to avoid anomalies or further analysis. But outliers can be interesting observations in themselves as they can be leading information to certain abnormal condition(s) just like the case of the recent discovery of obesity being a higher risk factor and prognosis to the novel COVID-19 pandemic. This study is focused on detecting outlying values of Body Mass Index (BMI) which are higher risk factors and prognosis of COVID-19 infections using the modified Multihalver technique for detecting outliers. The data of weights in kilogram (kg) and heights in meter (m) was collected from the records of a hospital and the Body Mass Index (BMI) was calculated as weight in kilogram divided by height in meter squared. The distribution of the computed BMI was fitted to the robust criteria of the modified Multihalver technique and the outlying values which are indices of underweight, overweight and obesity were detected as outliers. The study encourages obesity prevention at all ages and recommendation is on appropriate dieting to stay off the possible underlying diseases and in particular the novel COVID-19 pandemic.

Keywords: COVID-19 infections, body mass index, obesity, modified multihalver technique, outliers

1. Introduction

Worldwide, there are more than one billion overweight adults; at least three million of them are obese. Obesity and overweight poses a major risk for chronic diseases such as type 2 diabetes, cardiovascular disease, hypertension, stroke and certain forms of cancer (Williams *et al.* 2015) ^[12]. The main causes of higher Body Mass Index (BMI) are increased consumption of energy dense foods high in saturated fats and sugars and reduced physical activity. The prevalence of overweight and obesity is usually measured by using BMI defined as the weight in kilograms divided by the square of the height in meters (kg/m^2). A BMI of over 25 kg/m^2 is defined as overweight, and a BMI of over 30 kg/m^2 as obesity class

I. BMI over 35 kg/m^2 as obesity class.

II. BMI over 40 kg/m^2 as obesity class.

III. Or severe obesity.

BMI over 40 kg/m^2 as morbid obesity and BMI over 45 kg/m^2 classified as super obesity. However, BMI between 18 kg/m^2 – 25 kg/m^2 are considered normal and people with a BMI below 18.5 kg/m^2 tend to be under nutrition and are associated with ill health. These markers provide common benchmarks for assessment but the risks of disease in all populations can increase progressively from lower BMI levels. BMI is an indicator of the healthiness of an individual or otherwise on the nutrition scale (Astrup and Pedersen, 2011; Fock and Khoo, 2013) ^[1, 2]. BMI increases amongst middle-aged and elderly people, who are at the greater risk of health problems. In countries undergoing nutrition transition, over-nutrition often co-exists with under-nutrition. The distribution of BMI is shifting upwards in several populations. Recently, it has been shown that people who were undernourished in early life and then became obese in adulthood, tend to develop conditions such as high blood pressure, heart disease and diabetes

at an earlier age and in more severe form than those who were never undernourished (Fock and Khoo, 2013) [2]. Obesity is a major contributor to the global burden of chronic diseases and disability often co-exist in developing nations with under nutrition, a complex condition with serious social and psychological dimensions, affecting virtually all ages and socioeconomic groups. The consequences range from increased risk of premature death, to serious chronic conditions that reduce the overall quality of life. Of especial concern is the increasing incidence of child obesity which was not the case in the past.

The rising epidemic reflects the profound changes in society and behavioral patterns of communities over recent decades. While genes are important in determining a person's susceptibility to weight gain; energy balance is determined by calorie intake and physical activity. Therefore, societal changes and worldwide nutrition transition are driving the obesity epidemic. Economic growth, modernization, urbanization and globalization of food markers are just some of the forces thought to underlie the epidemic.

As the income rises and populations become more urban, diet high in complex carbohydrates has given way to more varied diets with a higher proportion of fats, saturated fats and sugars. At the same time, there are large shifts towards less physically demanding work have been observed worldwide. Moves towards less physical activity are also found in the increasing use of automated transport, technology in the home, and more passive leisure pursuits (Fock and Khoo, 2013) [2].

Most seriously and disturbing are the recent reports from studies across different countries showing the association of higher BMI and COVID-19 infections. People with overweight, obesity, cardiovascular diseases, hypercholesterolemia, hypertension, atherosclerosis, thrombosis and diabetes are at higher risk of COVID-19 infections. Coronavirus disease 2019 (COVID-19) is an infectious disease caused by severe acute respiratory syndrome coronavirus (SARS COVID-19 in China. COVID 19 is a disease caused by a new strain of Coronavirus. 'CO' stands for corona, 'VI' for virus and 'D' for disease. Formerly, this disease was referred to as '2019 novel coronavirus' or '2019 - nCov'. Kahn (2005) [5] confirmed that the history of human corona viruses began in 1965 and first characterized in the 1960s. The current scientific consensus is that the virus is most likely of zoonotic origin, from bats or another closely - related mammal.

The study of Karina CP, *et al.* (2020) [4] on Body Mass Index and prognosis of COVID-19 infections carried out a systematic review in order to investigate a possible association between body weight and prognosis among patient diagnosed with COVID-19. The outcome of their study shows that obesity is a higher risk factor and prognosis of COVID-19 infections. This study therefore is focused on detecting outlying values of BMI which are higher risk factors and prognosis of COVID-19 infections using the modified Multihalver technique for detecting outliers.

The detection of outlier(s) is often thought of as a means to eliminate such aberrant observation(s) from a set of data to avoid anomalies or further analysis. But outliers can be interesting observations in themselves as they can be leading information to certain abnormal condition(s) just like the case of the recent discovery of the outlying values of BMI as a higher risk factor and prognosis to the novel COVID-19 pandemic.

The study is aimed on detecting outlying values of BMI in a given distribution of BMI computed from a set of data on weights and heights of in - patients and out patients collected from Alpha Hospital, Nasarawa by using the robust criteria of modified Multihalver technique.

2. Materials and Method

2.1 The Modified Multihalver Technique (MMT)

The MMT is a robust parametric technique for detecting multiple outliers' in a large sample without masking and swamping effect (Usman and Shittu, 2013; Usman, 2015; Usman and Shittu, 2015) [7, 8, 10]. It is a modification of the Multihalver method of nominating outlier by Fernholz *et al.*, (2004) [13]. Multihalver method comes with myriads of limitations such as:

- Rigorous algorithm to detect outliers
- Perform well when sample size is small and even numbered. If sample is large it will required been broken into smaller sample sizes to function adequately
- It is not known to function in any known distribution. It is non - parametric based.
- It is a single outlier detector and so have problem of masking and swamping if there is more than one outlier in the data set.

Given the final matrix F_{k-1} as defined in equation (3.7.4) in the work of Usman (2015), i.e., $F_{k-1} = \Re(P_2)$, the Modified Multihalver Technique procedure consists of the following steps:

- To each observation y_i , we associate a mean where: $i = 1, \dots, n$. Each m_i is computed from the matrix F_{k-1} either from a column if i is even or from a row if i is odd. We make use of m_i, \dots, m_n to judge outlyingness.
- Obtain 20% trimmed mean (i. e. $\bar{m}_{0.20}$)
- Compute $a_i = |m_i - \bar{m}_{0.20}| - \min_{1 \leq i \leq n} |m_i - \bar{m}_{0.20}|$
- Compute the ordered sequence $a_{(1)} \leq a_{(2)} \leq \dots \leq a_{(n)}$ with the sequence of Gaussian quantiles: $g_i = -\Phi^{-1}\left(\frac{3i-1}{6n+2}\right)$ Via the ratio $q_i = \frac{a_i}{g_i}, i = 1, 2, \dots, n$
- Obtain the 20% trimmed mean of q_1, \dots, q_n i. e. $(\bar{q}_{0.20})$
- The observation y_i is declared an outlier if the test statistic;

$$\min_{j>i} \{q_i\} = \min_{j>i} \left\{ \frac{|a_i|}{|g_i|} \right\} > C\bar{q}_{0.5} \text{ holds}$$

The constant $C = 1.5$ is the reasonable multiplier of the critical value

2.2 Data Collection

The data set on weights (kg) and heights (m) of 93 in/out - patients of the Alpha Hospital, Nasarawa used for this research was collected from the records and statistics section of the hospital.

The computation of BMI was done using health calculator. BMI is a person's weight in kilogram divided by the square of the height in meters. The health calculator was employed for the purpose of speed and accuracy.

2.3 Determination of underweight, overweight and obesity

The body mass index (BMI) is currently the choice of measurement by many physicians and researchers studying obesity. The BMI uses a mathematical formula that accounts for both a person's weight and height. The BMI equals a person's weight in kilograms divided by height in meters squared ($BMI = kg/m^2$). It is important to understand what "healthy weight" means. Healthy weight is defined as a body mass index equals to or greater than 19 and less than 25 among all people 20 years of age or over. Generally obesity is defined as a BMI equal to or greater than 30.

The World Health Organization uses a classification system using BMI to define overweight and obesity as stated in the introduction and to be more specific as follow:

(<https://www.euro.who.int/en/health-topics/disease-prevention/nutrition/a-healthy-lifestyle/body-mass-index-bmi>)

- A BMI of 15 to 18 is defined as underweight (irrespective of age and gender)
- A BMI of 18.5 to 24.9 is defined as normal.
- A BMI of 25 to 29.9 is defined as a “pre-obese” (overweight)
- A BMI of 30 to 34.99 is defined as “obese class I”
- A BMI of 35 to 39.99 is defined as “obese class II”
- A BMI of or greater than 40.00 is defined as obese class III”
- A BMI of 45 to 50 is defined as “obese class IV” (morbidly obese)

- A BMI of 50 to 60 is defined as “obese class V” (super obese)
- A BMI of or greater than 60 is defined as “obese class VI” (hyper-obese)

3. Result and Discussion

The plots of the distribution of the BMI generated from the sets of data on weights and heights of patients are shown in in Fig 1 to 5. Common with the plots are data deviated considerably from normal. The outlying values fell outside of the range of BMI considered to be normal (i. e. BMI of 18.5 to 29.9).

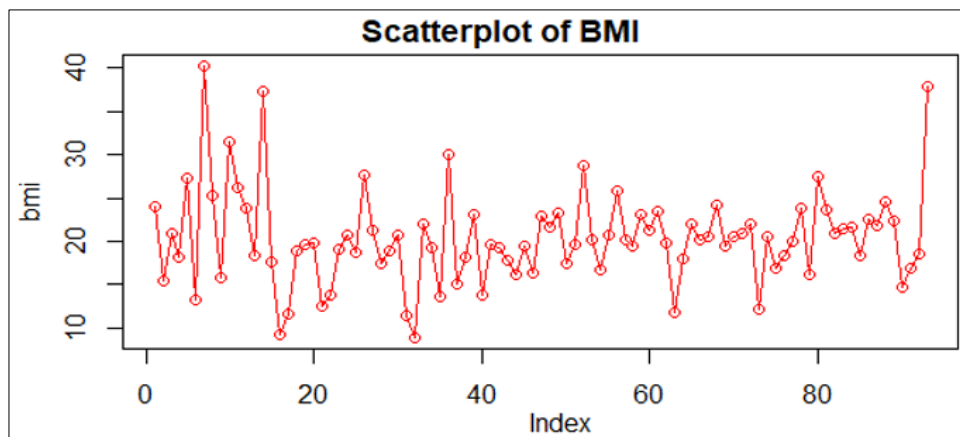


Fig 1: Scatter plot of BMI of the 93 patients showing evidence of outlying values of BMI

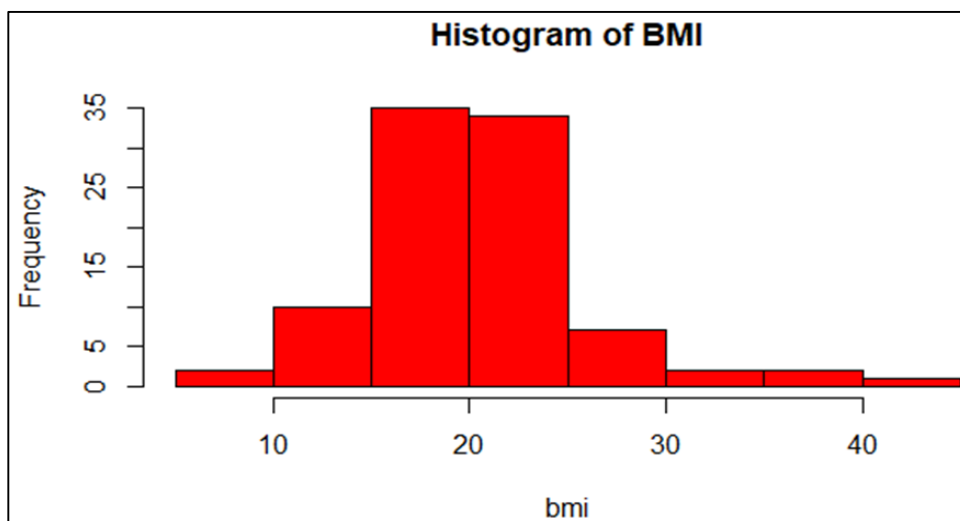


Fig 2: Histogram of BMI for the 93 patients showing evidence of deviation from normal as it is skewed to the right of the distribution

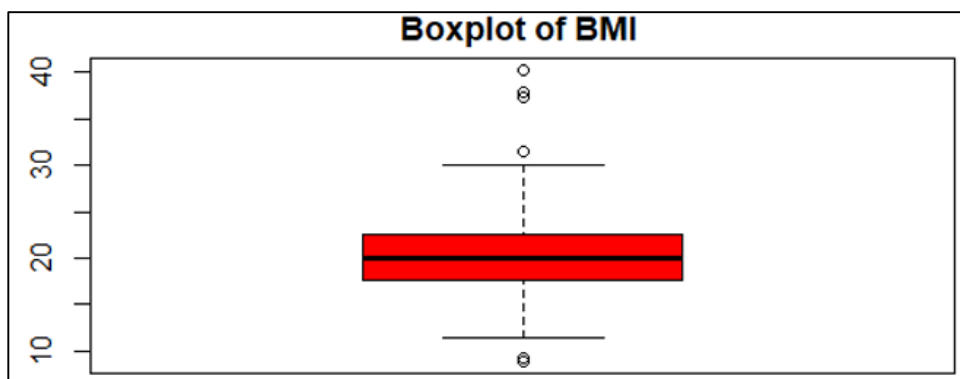


Fig 3: Box plot of BMI for the 93 patients showing evidence of outlying values of BMI at the lower and upper whiskers

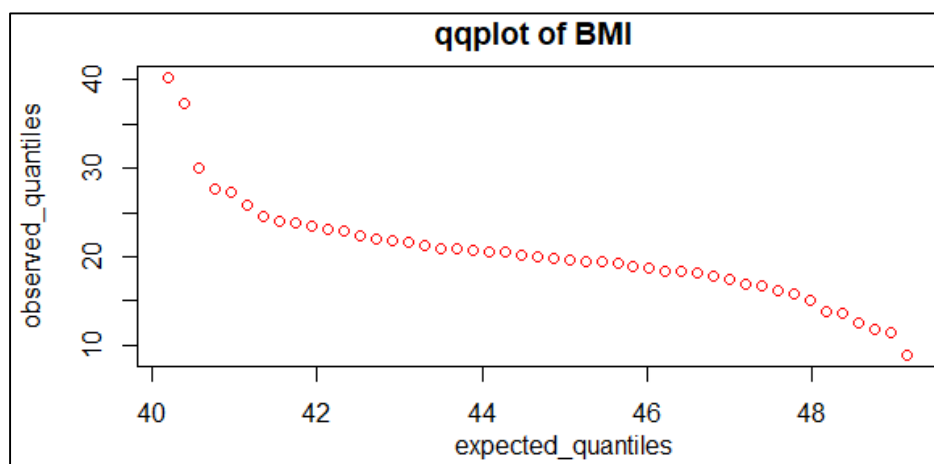


Fig 4: The QQ Plot of BMI for the 93 patients showing evidence of outlying values of BMI

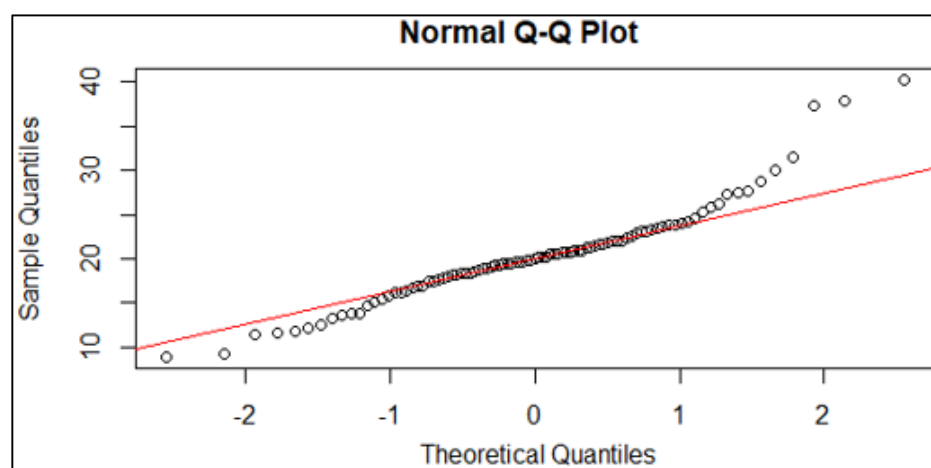


Fig 5: Normal QQ plot of BMI for the 93 patients showing evidence of outlying values of BMI at the lower and upper quintiles

Table 1: Analysis of data set of size 93 based on the performance of the robust criteria of MMT $P=0.2$, $C=1.5$, $n=93$, $\bar{M}_p=18.6$, $\bar{q}_{0.2}=5.83$, $K = np = 18.6$, minimum value =, Highest value =

Y	m_i	$ m_i - \bar{m}_{0.2} $	$ a_i $	ϕ^{-1}	g_i	q_i	$c\bar{q}_{0.2}$	Decision
1	24.08*	5.48	5.33	0.00	0.5	10.66	8.745	Declared
2	15.48	3.12	2.97	0.00	0.5	5.94	8.745	Not
3	20.93	2.33	2.18	0.01	0.5040	4.33	8.745	Not
4	18.16	0.44	0.29	0.02	0.5080	0.57	8.745	Not
5	27.27	8.67	8.52	0.03	0.5120	16.64	8.745	Declared
6	13.34	5.26	5.11	0.03	0.5120	9.98	8.745	Declared
7	40.19	21.59	21.44	0.04	0.1600	41.55	8.745	Declared
8	25.19	6.59	6.44	0.04	0.5160	12.48	8.745	Declared
9	15.78	2.82	2.67	0.05	0.5199	5.14	8.745	Not
10	31.47	12.87	12.72	0.05	0.5199	24.47	8.745	Declared
11	26.23	7.63	7.48	0.06	0.5239	14.28	8.745	Declared
12	23.87	5.12	5.12	0.06	0.5239	9.68	8.745	Declared
13	18.37	0.23	0.05	0.07	0.5279	0.09	8.745	Not
14	37.3	18.7	18.55	0.07	0.5279	35.14	8.745	Declared
15	17.57	1.03	0.88	0.08	0.5319	1.65	8.745	Not
16	9.21	9.39	9.24	0.08	0.5319	17.37	8.745	Declared
17	11.69	6.91	6.76	0.09	0.5359	12.61	8.745	Declared
18	18.96	0.36	0.21	0.1	0.5398	0.39	8.745	Not
19	19.69	1.09	0.94	0.1	0.5398	1.74	8.745	Not
20	19.89	1.27	1.12	0.11	0.5438	2.06	8.745	Not
21	12.47	6.13	5.98	0.11	0.5438	11.0	8.745	Declared
22	13.79	4.81	4.66	0.12	0.5517	8.51	8.745	Not
23	19.13	0.53	0.38	0.12	0.5478	0.69	8.745	Not
24	20.8	2.2	2.05	0.13	0.5478	3.72	8.745	Not
25	18.75	0.15	0	0.13	0.5517	0	8.745	Not
26	27.68	9.04	8.89	0.14	0.5517	16.0	8.745	Declared
27	21.35	2.75	2.6	0.14	0.5557	4.68	8.745	Not
28	17.44	1.16	1.01	0.1	0.5557	1.80	8.745	Not
29	18.83	0.26	0.11	0.15	0.5596	0.20	8.745	Not

30	20.66	2.06	1.91	0.16	0.5636	3.39	8.745	Not
31	11.42	7.18	7.03	0.16	0.5636	12.47	8745	Declared
32	8.95	9.65	9.5	0.17	0.5675	16.74	8.745	Declared
33	22.06	3.46	3.31	0.18	0.5714	5.79	8.745	Not
34	19.28	0.68	0.53	0.18	0.714	0.93	8745	Not
35	13.67	4.93	4.78	0.19	0.5753	8.31	8.745	Not
36	30.01	11.41	11.26	0.19	0.5753	19.57	8.745	Declared
37	15.09	3.51	3.66	0.20	0.5793	6.32	8.745	Not
38	18.19	0.41	0.26	0.20	0.5793	0.45	8.745	Not
39	23.1	4.5	4.35	0.21	0.5832	7.46	8.745	Not
40	13.85	4.75	4.6	0.21	0.5832	7.89	8.745	Not
41	19.69	1.09	0.94	0.22	0.5871	1.86	8.745	Not
42	19.33	0.73	0.58	0.22	0.5871	0.99	8.745	Not
43	17.81	0.79	0.64	0.23	0.5910	1.08	8.745	Not
44	16.21	2.39	2.24	0.23	0.5910	3.79	8.745	Not
45	19.54	0.94	0.79	0.24	0.5948	1.33	8.745	Not
46	16.18	2.18	2.03	0.25	0.5987	3.39	8.745	Not
47	22.9	4.3	4.15	0.25	0.5987	6.93	8.745	Not
48	21.66	3.06	2.91	0.26	0.6026	4.83	8.745	Not
49	23.24	4.64	4.49	0.26	0.6026	7.45	8.745	Not
50	17.4	1.2	1.05	0.27	0.6064	1.73	8.745	Not
51	19.57	0.97	0.82	0.27	0.6064	1.35	8.745	Not
52	28.81	10.21	10.06	0.28	0.6103	16.48	8.745	Declared
53	20.19	1.59	1.44	0.28	0.6103	2.36	8.745	Not
54	16.66	1.94	1.79	0.29	0.6141	2.91	8.745	Not
55	20.81	2.21	2.06	0.29	0.6141	3.35	8.745	Not
56	25.74	7.14	6.99	0.30	0.6179	11.31	8.745	Declared
57	20.18	1.58	1.43	0.30	0.6179	2.31	8.745	Not
58	19.42	0.82	0.67	0.31	0.6217	1.08	8.745	Not
59	23.01	4.41	4.26	0.31	0.6217	6.85	8.745	Not
60	21.27	2.67	2.52	0.32	0.6255	4.03	8.745	Not
61	23.51	4.91	4.76	0.33	0.6293	7.56	8.745	Not
62	19.9	1.3	1.15	0.33	0.6293	1.83	8.745	Not
63	11.8	6.8	6.65	0.34	0.6331	10.50	8.745	Declared
64	18.02	0.58	0.43	0.34	0.6331	0.68	8.745	Not
65	21.99	3.39	3.24	0.35	0.6368	5.09	8.745	Not
66	20.16	1.56	1.41	0.35	0.6368	2.21	8.745	Not
67	20.57	1.97	1.82	0.36	0.6406	2.84	8.745	Not
68	24.15	5.55	5.4	0.36	0.6406	8.43	8.745	Not
69	19.48	0.88	0.73	0.37	0.6443	1.13	8.745	Not
70	20.59	1.99	1.84	0.38	0.6480	0.59	8.745	Not
71	20.84	2.24	2.09	0.38	0.6480	3.23	8.745	Not
72	22.04	3.44	3.29	0.39	0.6517	5.05	8.745	Not
73	12.18	6.42	6.27	0.40	0.6554	9.57	8.745	Declared
74	20.57*	16.03	15.91	0.40	0.6554	24.26	8.745	Declared
75	16.89	1.71	1.56	0.40	0.6554	2.38	8.745	Not
76	18.37	0.23	0.18	0.41	0.6591	0.27	8.745	Not
77	19.93	1.33	1.18	0.41	0.6591	1.09	8.745	Not
78	23.79	5.19	5.04	0.42	0.6628	7.60	8.745	Not
79	16.2	2.4	2.25	0.42	0.6628	3.39	8.745	Not
80	27.41	8.81	8.66	0.43	0.6664	13.0	8.745	Declared
81	23.63	5.03	4.88	0.43	0.6664	7.32	8.745	Not
82	20.86	2.26	2.11	0.44	0.6700	3.15	8.745	Not
83	21.39	2.79	2.64	0.44	0.6700	3.94	8.745	Not
84	21.63	3.03	2.88	0.45	0.6736	4.28	8.745	Not
85	18.34	0.26	0.11	0.45	0.6736	0.16	8.745	Not
86	22.56	3.96	3.81	0.46	0.6772	5.63	8.745	Not
87	21.81	3.21	3.06	0.47	0.6808	4.50	8.745	Not
88	24.5	5.9	5.75	0.45	0.6808	8.45	8.745	Not
89	22.43	3.83	3.68	0.48	0.6844	5.38	8.745	Not
90	14.8	3.8	3.65	0.48	0.6844	5.33	8.745	Not
91	16.98	1.62	1.47	0.49	0.6879	2.14	8.745	Not
92	18.78	0.18	0.03	0.49	0.6879	0.04	8.745	Not
93	37.87	17.53	17.38	0.50	0.6915	25.13	8.745	Declared

Source: Results of the analysis of MMT Observation

$Y_1, Y_5, Y_6, Y_7, Y_{10}, Y_{11}, Y_{12}, Y_{14}, Y_{16}, Y_{17}, Y_{21}, Y_{26}, Y_{26}, Y_{31}, Y_{32}, Y_{36}, Y_{52}, Y_{56}, Y_{63}, Y_{73}, Y_{74}, Y_{80}, Y_{93}$ (23 observations) were declared outliers. Meaning that 23 of the 93 BM I of patients were declared outlying. From Table 1,

the values of BMI declared by MMT actually fell out of the range of BMI defined as normal.

Table 2: Summary of the performance of MMT

S/N	Description	Count	Percentage
1	Observation	93	100
2	Outlying values	23	24.7
3	Underweight	10	10.75
4	Overweight	10	10.75
5	Obese class I	3	2.2
6	Obese class II	Nil	Nil
7	Obese class III	“	“
8	Obese class IV	“	“
9	Obese class V	“	“
10	Obese class VI	“	“

Source: Results of the analysis of MMT in Table 1

Data set: Body Mass Index (BMI), Minimum Value: 8.95 Maximum Value: 40.19

4. Conclusion

The performance of the robust criteria of Modified Multihalver Technique was ascertained in this study. The twenty three (23) outlying values of Body Mass Index (BMI) detected by MMT were 100% in agreement with World Health Organization's classification system of BMI as defined. The Modified Multihalver Technique is no doubt an efficient method of multiple outlier detection without threshold, masking and swamping effect.

5. Recommendation

- The Modified Multihalver Technique should be adopted in the field of public health as risk detector because of its efficiency as proven in this study.
- Persons who are obese as discussed in this paper are recommended to be conversant with the safety protocols of COVID-19 since obesity have been confirmed to be a risk factor of COVID-19 and a predictor of mortality.
- To avoid higher BMI, Discipline and control of diet with high proportion of fats, saturated fats, sugar and involvement in regular physical activity is highly recommended.

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